

$$J(w) = \frac{1}{2m} \sum_{i=0}^m (\hat{y}_i - y_i)^2$$

$$J(1) = \frac{1}{2m} (0^2 + 0^2 + 0^2)$$

$$= 0$$

$$J(0.5) = \frac{1}{2m} [(0.5 - 1)^2 + (1 - 2)^2 + (1.5 - 3)^2]$$

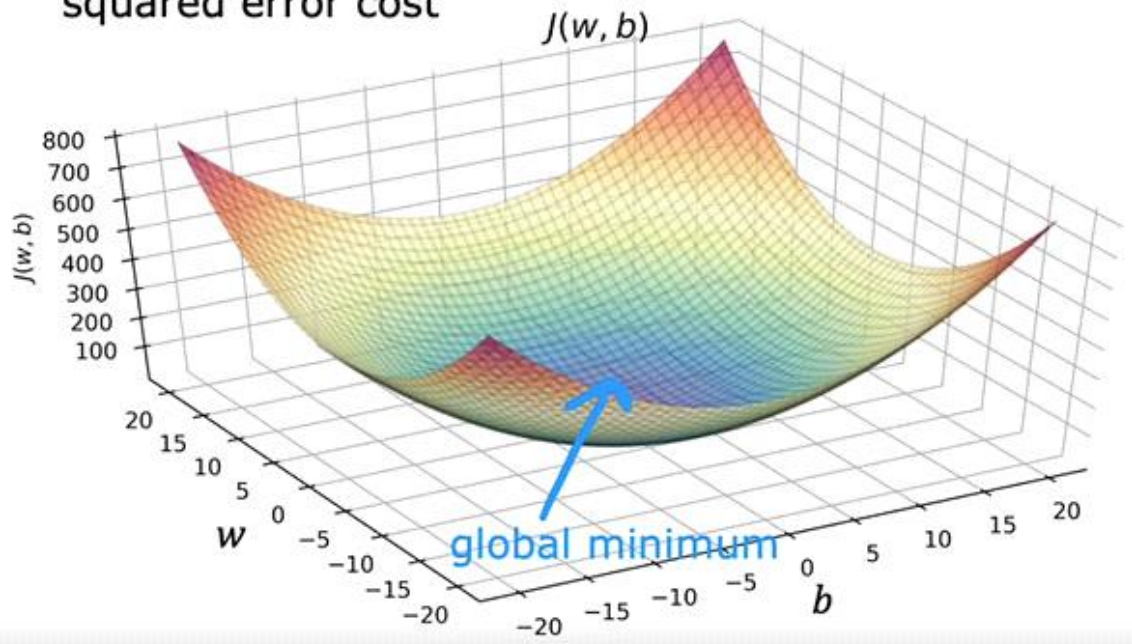
$$= \frac{1}{2 \times 3} [3 \cdot 5]$$

$$= 0.58$$

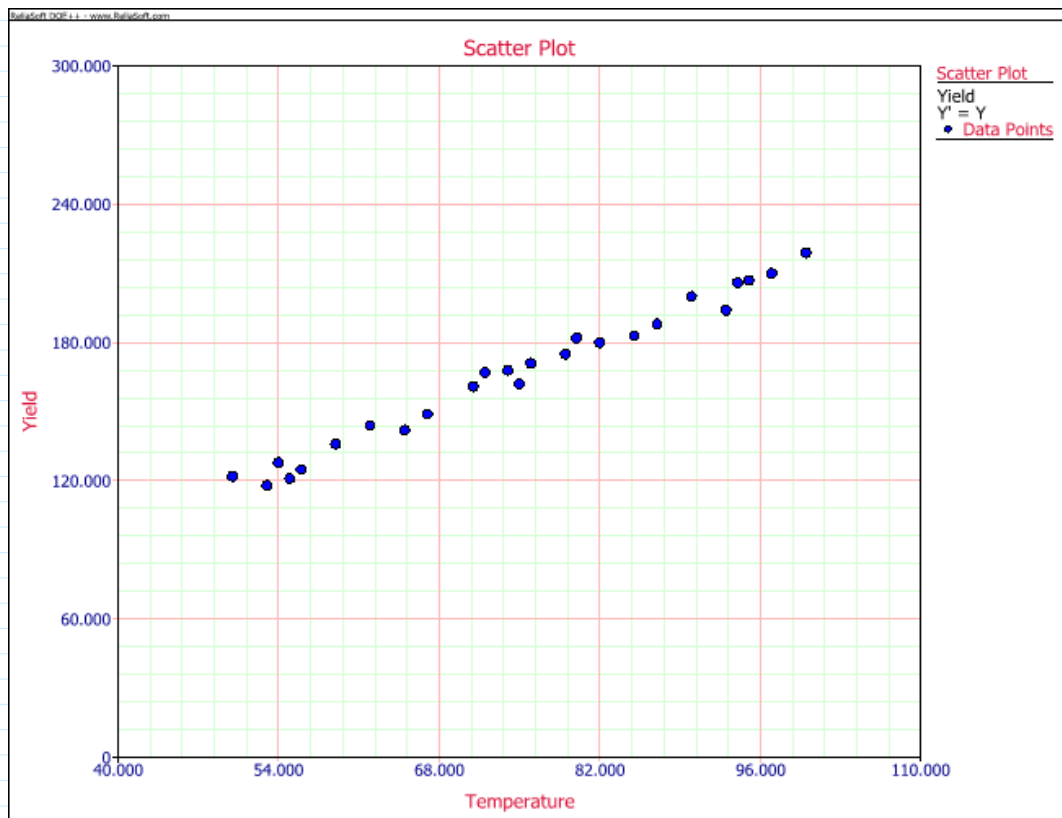
$$J(0) =$$

but $J(w, b)$ is a two parameters function.

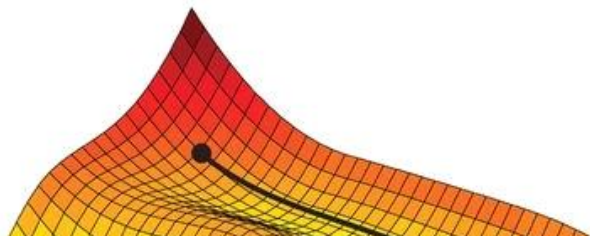
squared error cost

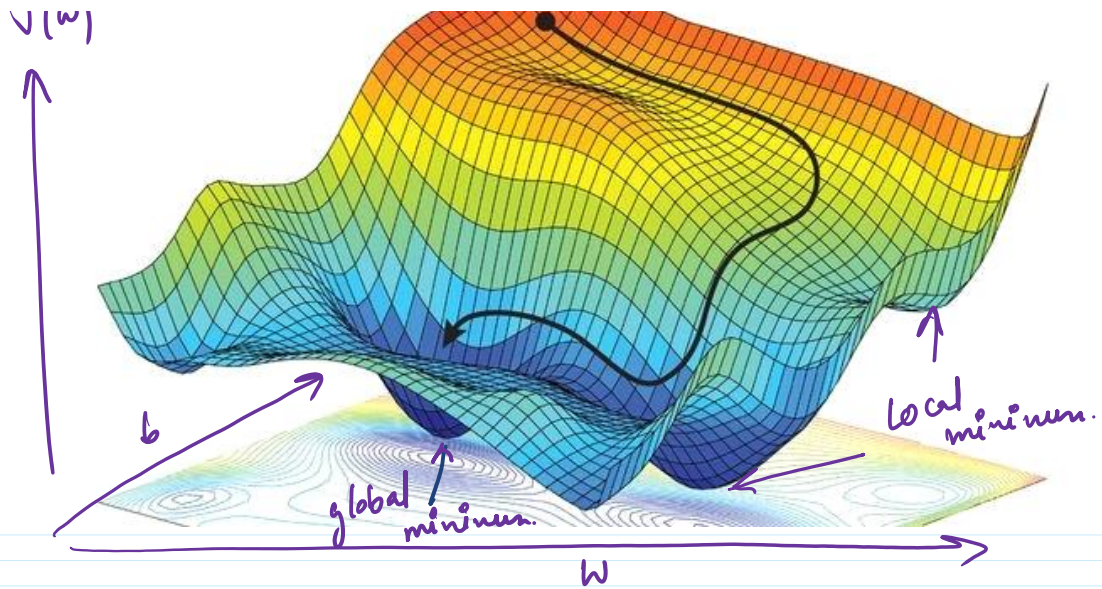


Linear Regression



$\nabla(w)$
 \uparrow





Neural Network :- $J(w_1, w_2, w_3, \dots, b)$
 (Not a squared error cost function)

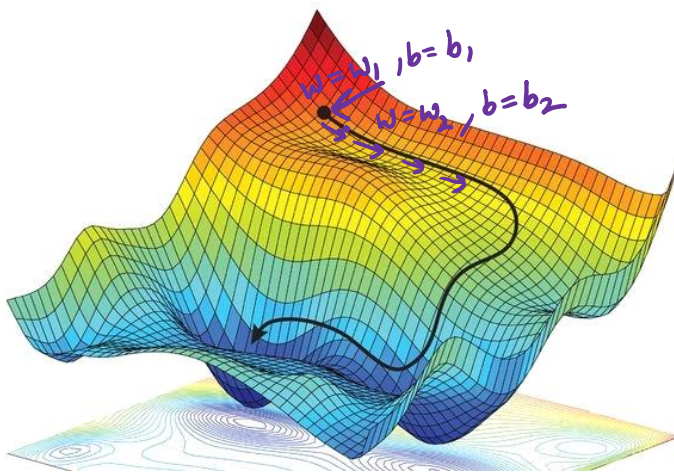
Goal :- For function $J(w, b)$
 we want $\min_{w, b} J(w, b)$

Outline :-

Start with some initial values of w, b .

(let $w=0, b=0$)

keep changing w, b to reduce $J(w, b)$
 until we find minimum or nearest min.



Gradient Descent Algorithm :-

Repeat until convergences

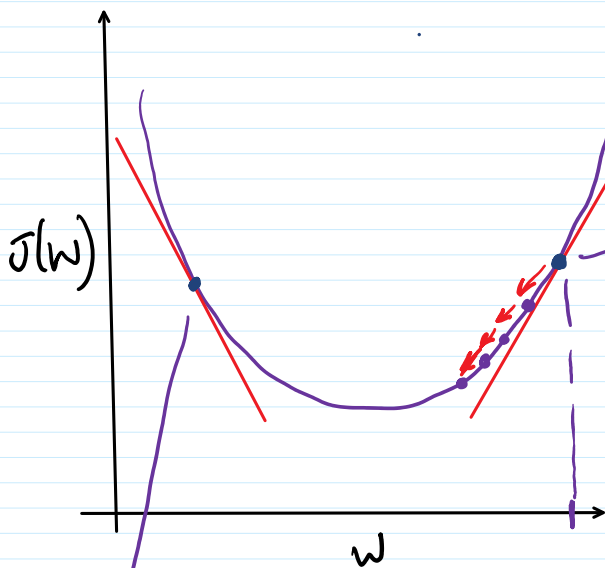
$$\left\{ \begin{aligned} w &= w - \alpha \frac{\partial}{\partial w} J(w, b) \end{aligned} \right.$$

$$\left. \begin{aligned} b &= b - \alpha \frac{\partial}{\partial b} J(w, b) \end{aligned} \right\}$$

$\alpha \rightarrow$ learning rate

$\frac{\partial}{\partial w} J(w, b) \rightarrow$ derivative of $J(w)$

$\frac{\partial}{\partial b} J(w, b) \rightarrow$ derivative of $J(b)$



$$w = w - \alpha \underbrace{\frac{d}{dw} J(w)}_{> 0}$$

$$w = w - \alpha \cdot (+ve)$$

$$w = w - (+ve)$$

$w \downarrow$ decreasing

$$w = w - \alpha \underbrace{\frac{d}{dw} J(w)}_{< 0}$$

$$w = w - \alpha \cdot (-ve)$$

$= W - (ue)$
with increasing

illy for "b".

Choosing " α ".

