

Möller-Trumbore Algorithm :-

A faster ray-triangle intersection algorithm.  
 (1997)

Using barycentric coordinates equations,

$$P = wA + uB + vC \quad \text{--- ①}$$

also  $w + u + v = 1$

$$\Rightarrow w = 1 - u - v \quad \text{--- ②}$$

Using ② in ①

$$P = (1 - u - v)A + uB + vC$$

$$P = A - Au - Av + uB + vC$$

$$P = A + u(B - A) + v(C - A) \quad \text{--- ③}$$

$(B - A) \rightarrow$  AB edge

$(C - A) \rightarrow$  AC edge

Also,  $P = O + tD$

using in ③

$$O + tD = A + u(B - A) + v(C - A)$$

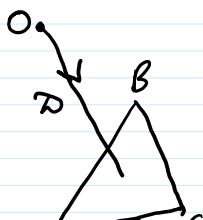
$$O - A = -tD + u(B - A) + v(C - A)$$

$$\underbrace{\begin{bmatrix} -D & (B-A) & (C-A) \end{bmatrix}}_{\text{known}} \underbrace{\begin{bmatrix} t \\ u \\ v \end{bmatrix}}_{\text{unknowns}} = \underbrace{(O-A)}_{\text{known}}$$

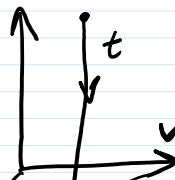
where  $-D$ ,  $(B - A)$ ,  $(C - A)$ ,  $(O - A)$   
 are vectors

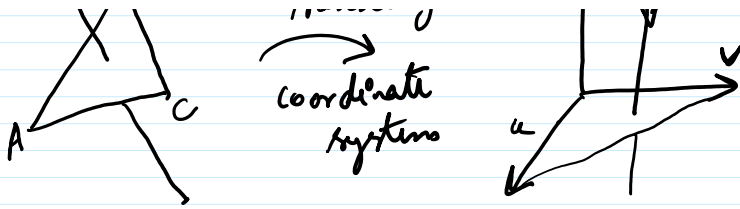
$t, u, v$  are scalar quantities

$t$  distance from ray to intersection point  
 $u, v$  barycentric coordinates



translating  
 coordinate





Using Cramer's Rule,

$$\begin{bmatrix} t \\ u \\ v \end{bmatrix} = \frac{1}{\begin{vmatrix} -D & B-A & C-A \end{vmatrix}} \begin{bmatrix} \begin{vmatrix} 0-A & B-A & C-A \end{vmatrix} \\ \begin{vmatrix} -D & 0-A & C-A \end{vmatrix} \\ \begin{vmatrix} -D & B-A & 0-A \end{vmatrix} \end{bmatrix}$$

$$|ABC| = (A \times C) \cdot B = (C \times B) \cdot A$$

$$= \frac{1}{(D \times (C-A)) \cdot (B-A)} \begin{bmatrix} ((0-A) \times (C-A)) \cdot (B-A) \\ (-D \times (C-A)) \cdot (0-A) \\ (-D \times (0-A)) \cdot (B-A) \end{bmatrix}$$

$\Rightarrow$   $t, u, v$  can be calculated using cross and dot products between vertices of the triangle, origin and the ray direction.

Advantage :-

Plane equations need not be computed on the fly or stored.

# Fast, Minimum Storage Ray/Triangle Intersection

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## Abstract

We present a clean algorithm for determining whether a ray intersects a triangle. The algorithm translates the origin of the ray and then changes the base of that vector which yields a vector  $(t \ u \ v)^T$ , where  $t$  is the distance to the plane in which the triangle lies and  $(u, v)$  represents the coordinates inside the triangle.

One advantage of this method is that the plane equation need not be