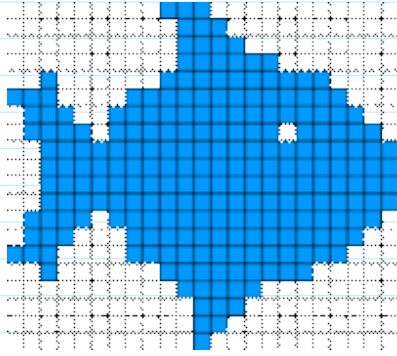


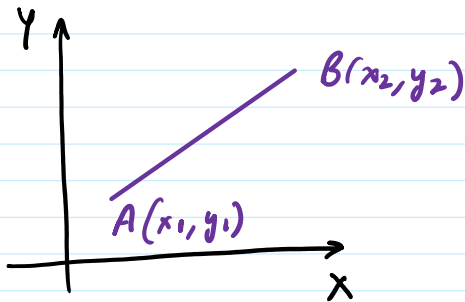
## Rasterization / Scan Conversion :-

Representation of continuous graphics objects as a collection of discrete pixels.



## Scan Conversion of a Line :-

Line :-



Equation of line,

$$y = mx + c$$

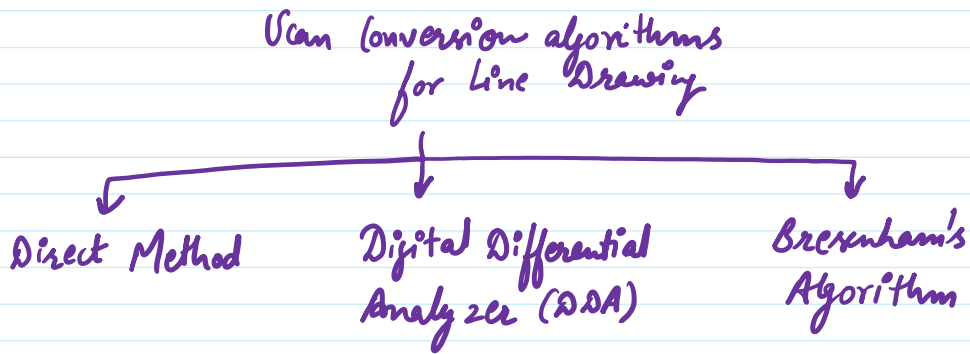
$$m = \Delta y / \Delta x$$

$$\Delta x = x_2 - x_1$$

$$\Delta y = y_2 - y_1$$

Using scan conversion algorithms, line is drawn by plotting the

pixels in sequence.



### Direct Method:-

Two known end points

↓  
Find other points lying on the line using  $y = mx + c$

### Algorithm :-

- ① Read  $P_1(x_1, y_1)$  and  $P_2(x_2, y_2)$
- ② Calculate
$$dx = x_2 - x_1$$
$$dy = y_2 - y_1$$
- ③ Calculate slope
$$m = dy/dx$$
- ④ Set  $(x, y)$  to starting point
  - if  $dx > 0$  then
    - $x = x_1$
    - $y = y_1$
    - $x_{end} = x_2$
  - if  $dx < 0$  then

$$x = x_2$$

$$y = y_2$$

$$x_{end} = x_2$$

⑤ Now calculate

$$C = y - mx$$

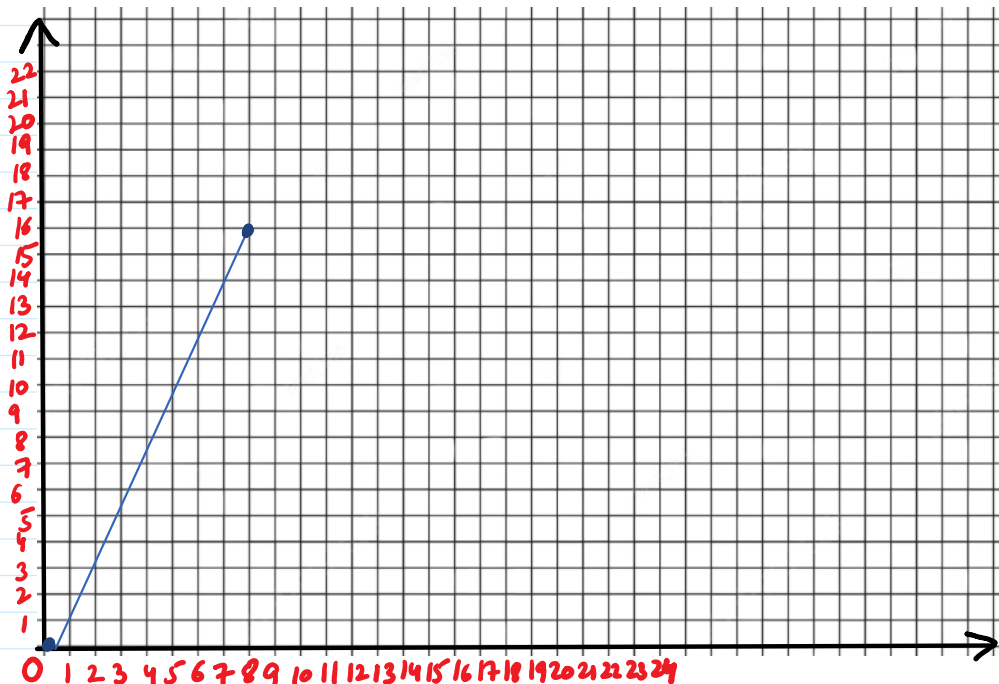
⑥ Plot a point at current  $(x, y)$  coordinates.

⑦ Increment  $x$ ,  $x = x + 1$

⑧ Compute  $y$ ,  $y = mx + C$

⑨ If  $x = x_{end}$  then stop  
otherwise Go to ⑥

Q8- Draw a line using direct method  
between points  $(0, 0)$  &  $(8, 16)$



①  $(x_1, y_1)$   $(x_2, y_2)$

(0,0) and (8,16)

②  $dx = 8 - 0 = 8$  ,  $dy = 16 - 0 = 16$ .

③  $m = dy/dx = 16/8 = 2$ .

④ Set initial point (x,y)

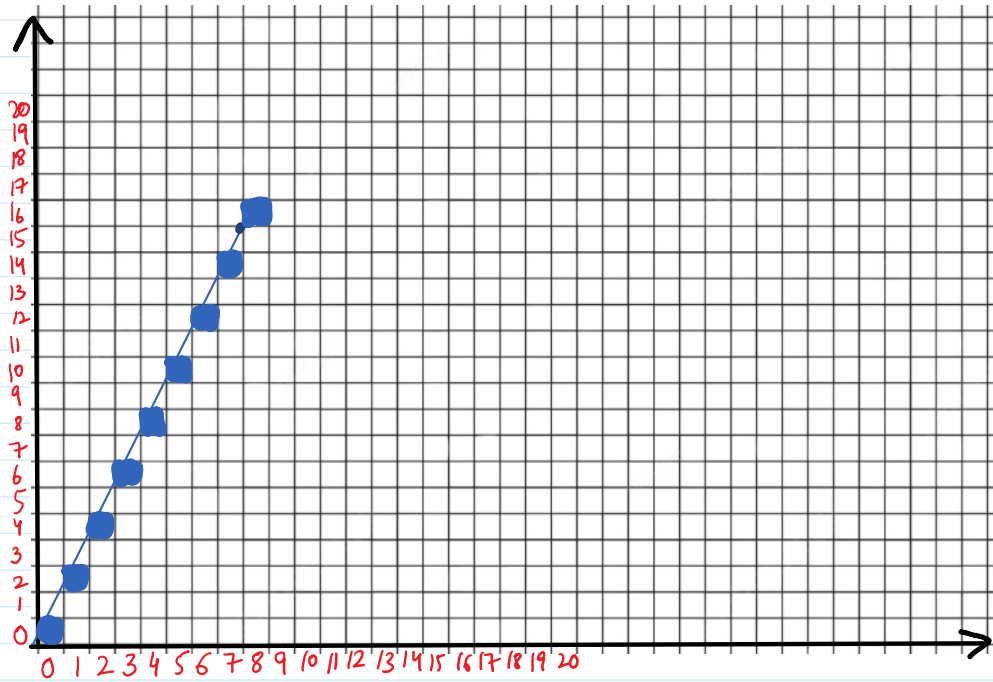
$dx > 0$

$\Rightarrow x = 0$   $y = 0$   $x_{end} = 8$

⑤ Calculate  $c = y - mx$   $c = 0$

While  $x = x_{end}$

$x = x + 1$	$y = mx + 0$	Points
0	0	$P_1(0, 0)$
1	2	$P_2(1, 2)$
2	4	$P_3(2, 4)$
3	6	$P_4(3, 6)$
4	8	$P_5(4, 8)$
5	10	$P_6(5, 10)$
6	12	$P_7(6, 12)$
7	14	$P_8(7, 14)$
8	16	$P_9(8, 16)$



## ② Digital Differential Analyzer (DDA)

①  $P_1(x_1, y_1)$  and  $P_2(x_2, y_2)$

② Finding appropriate length of the line

if  $(\text{abs}(x_2 - x_1) > \text{abs}(y_2 - y_1))$  then

$$\text{Length} = \text{abs}(x_2 - x_1)$$

otherwise

$$\text{Length} = \text{abs}(y_2 - y_1)$$

③ Find raster unit

$$dx = (x_2 - x_1) / \text{Length}$$

$$dy = (y_2 - y_1) / \text{Length}$$

floating point calculations

④ set  $x = x_1$ ,  $y = y_1$  and  $i = 0$

⑤ Plot  $(x, y)$

- ⑤ Plot  $(x, y)$   
 $x = x + dx$   
 $y = y + dy$
- ⑥ Repeat ⑤ until  $i \leq \text{length}$

Example :-  $(0, 0)$  to  $(8, 8)$

①  $x_1 = 0$   $y_1 = 0$   $x_2 = 8$   $y = 8$

②  $\text{abs}(x_2 - x_1) = 8$   
 $\text{abs}(y_2 - y_1) = 8$   
 $\text{length} = 8$

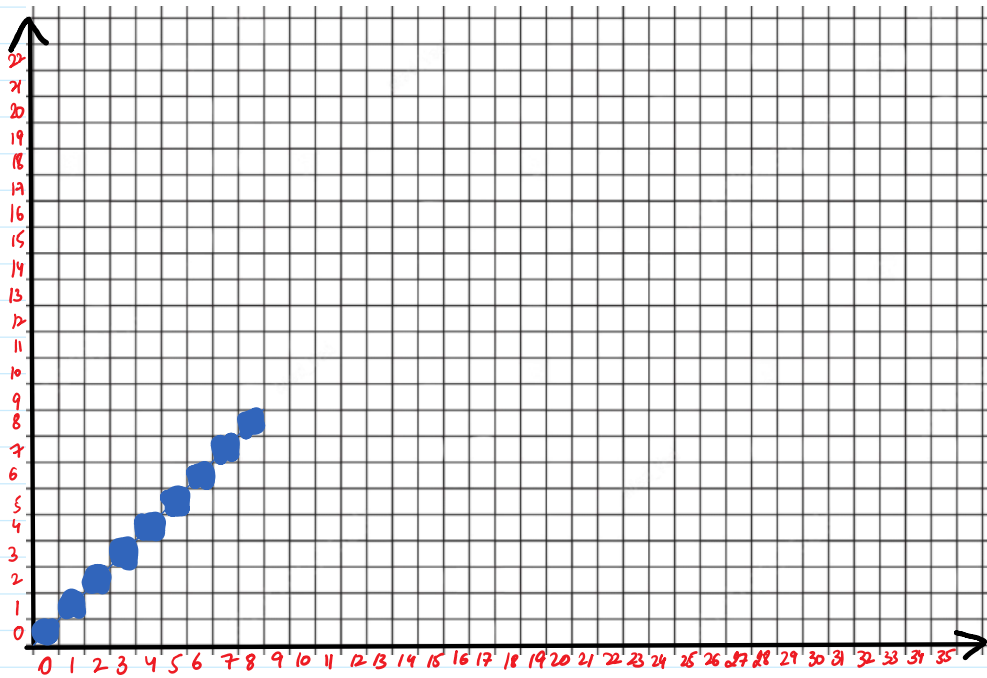
③  $dx = 1$   
 $dy = 1$

④ Set  $(x, y)$   $x = 0$ ,  $y = 0$

⑤ Execute until  $i \leq \text{length}$

$i$	$x$	$y$	points
0	0	0	(0,0)
1	1	1	(1,1)
2	2	2	(2,2)
3	3	3	(3,3)
4	4	4	(4,4)
5	5	5	(5,5)
6	6	6	(6,6)
7	7	7	(7,7)
8	8	8	(8,8)

8 | 8 | 8 | (8,8)

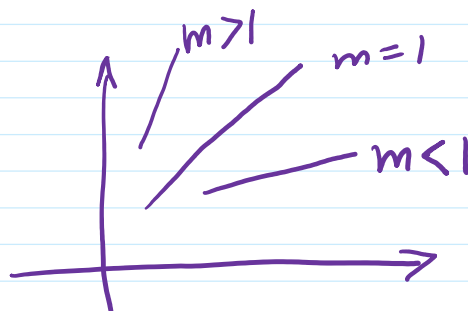


"Floating Point Calculations"

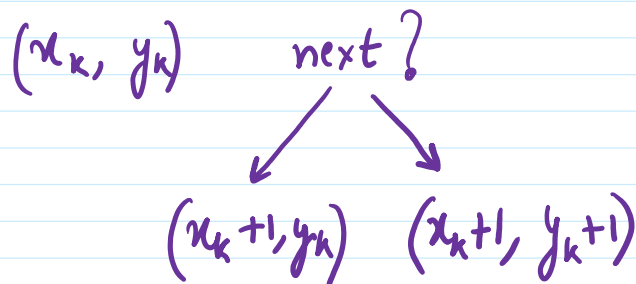
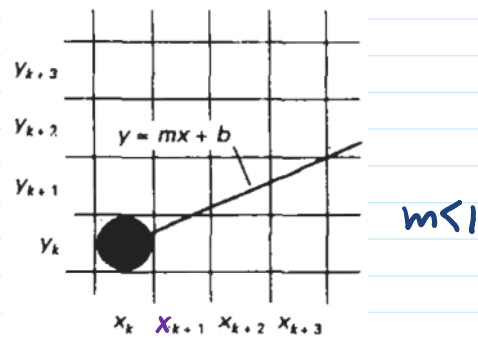
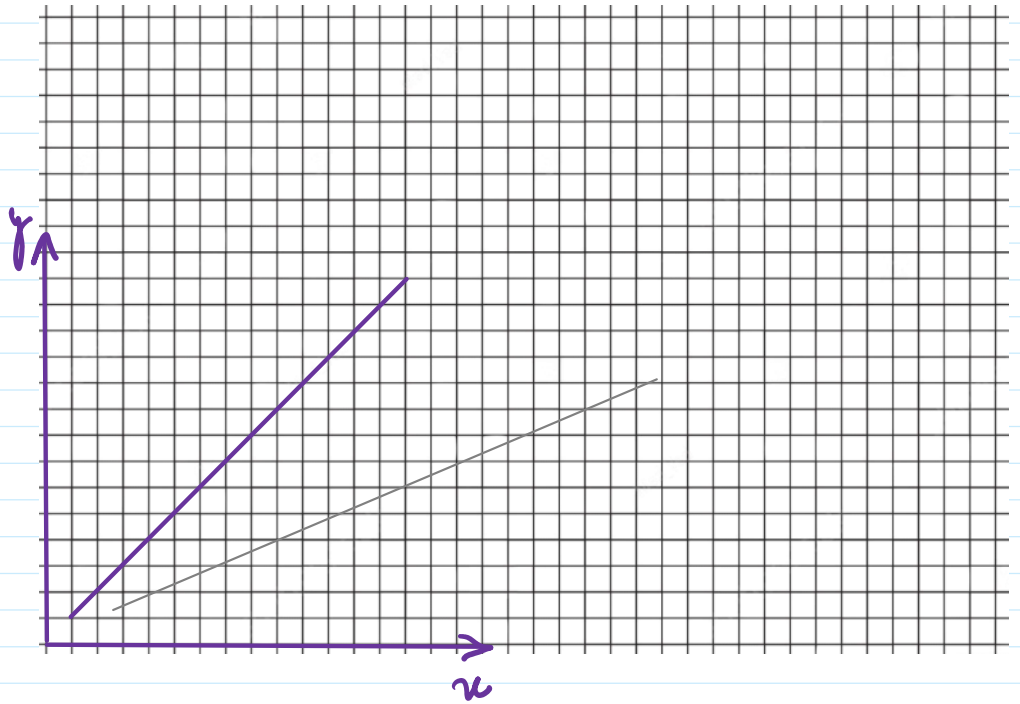
### ③ Bresenham's Line Algorithm

Jack Elton Bresenham, 1962  
(IBM)

Using only integer calculations.



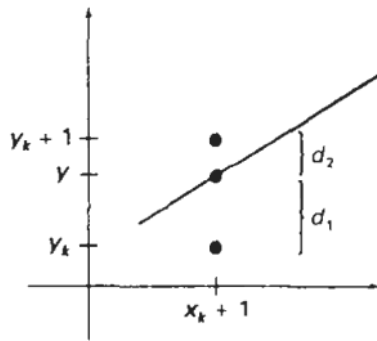
For slope  $m < 1$ ,  
sampling at unit  $x$  intervals.



$$y = m(x_k + 1) + b$$



At  $x_{k+1}$ , separating pixel from line,



from figure,

$$\begin{aligned}d_1 &= y - y_k \\ &= m(x_k + 1) + b - y_k\end{aligned}$$

and

$$\begin{aligned}d_2 &= (y_k + 1) - y \\ &= y_k + 1 - m(x_k + 1) - b\end{aligned}$$

$$d_1 - d_2 = 2m(x_k + 1) - 2y_k + 2b - 1$$

$$\boxed{m = \Delta y / \Delta x}$$

$$P_k = (d_1 - d_2)\Delta x = 2\Delta y \cdot x_k - 2\Delta x \cdot y_k + C$$

$$P_{k+1} = 2\Delta y \cdot x_{k+1} - 2\Delta x \cdot y_{k+1} + C$$

$$P_{k+1} - P_k = 2\Delta y(x_{k+1} - x_k) - 2\Delta x(y_{k+1} - y_k)$$

$$\text{but } x_{k+1} = x_k + 1$$

$$P_{k+1} = P_k + 2\Delta y - 2\Delta x \underbrace{(y_{k+1} - y_k)}$$

↙ ↘  
0 1

Algorithm :-

①  $P_1(x_1, y_1)$  and  $P_2(x_2, y_2)$

② Calculate

$$dx = x_2 - x_1$$

$$dy = y_2 - y_1$$

③ Calculate decision parameter  $P$

$$P = 2dy - dx$$

④ Set initial point

$$x = x_1, y = y_1$$

$$\text{and } i = 0$$

⑤ Plot  $(x, y)$

if  $P < 0$  then

$$x = x + 1$$

$$P = P + 2dx$$

else

$$x = x + 1$$

$$y = y + 1$$

$$P = P + 2dy - 2dx$$

⑥ Repeat ⑤ until  $i \leq dx$

Example :- Draw  $(20, 10)$  and  $(30, 18)$

①  $(20, 10)$  &  $(30, 18)$

$$x_1 = 20 \quad y_1 = 10 \quad x_2 = 30 \quad y_2 = 18$$

$$\textcircled{2} \quad dx = x_2 - x_1 = 10$$

$$dy = y_2 - y_1 = 8$$

$\textcircled{3}$  Decision parameter

$$p = 2dy - dx$$

$$= 6$$

$\textcircled{4}$  Set  $(x, y)$

$$x = x_1 = 20$$

$$y = y_1 = 10$$

$$\text{and } i = 0$$

$\textcircled{5}$  Execute until  $i \leq dx$

$i$	$p$	Points
0		(20, 10)
1	6	(21, 11)
2	2	(22, 12)
3	-2	(23, 12)
4	14	(24, 13)
5	10	(25, 14)
6	6	(26, 15)
7	2	(27, 16)
8	-2	(28, 16)
9	14	(29, 17)
10	10	(30, 18)

